

# Exoplanetary Microlensing science with WFIRST

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**NPP Fellows @ JPL**  
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# *WFIRST* Microlensing Primer Series

- I. Basic Introduction to the Methodology and Theory of Gravitational Microlensing Searches for Exoplanets  
W, 21/Sept , Yossi Shvartzvald
- II. Lens Companion Detection and Characterization  
W, 28/Sept , Yossi Shvartzvald
- III. Results from and Future Directions for **Ground**-based Microlensing Surveys  
W, 12/Oct , Calen Henderson
- IV. Results from and Future Directions for **Space**-based Microlensing Surveys (including *WFIRST*)  
W, 19/Oct , Calen Henderson

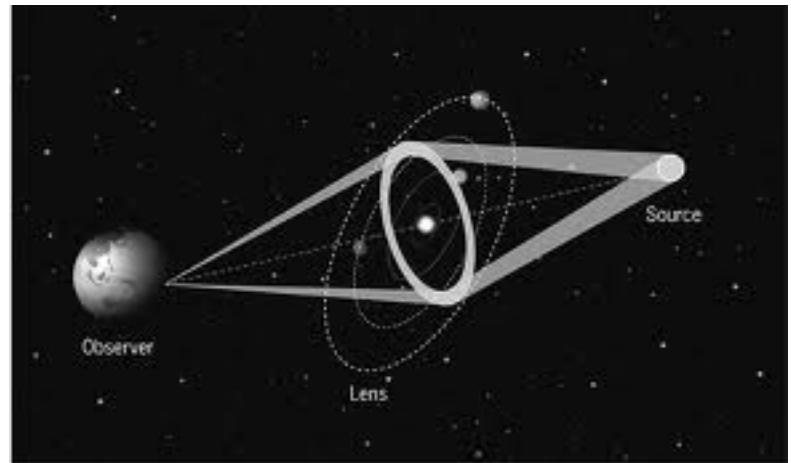
# Microlensing basics

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# Microlensing basics

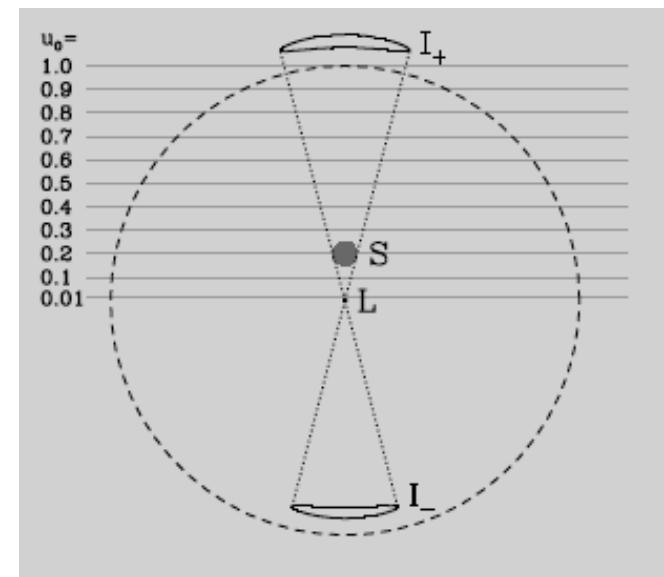
Amplification =  $\frac{\text{image area}}{\text{source area}}$

$$A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

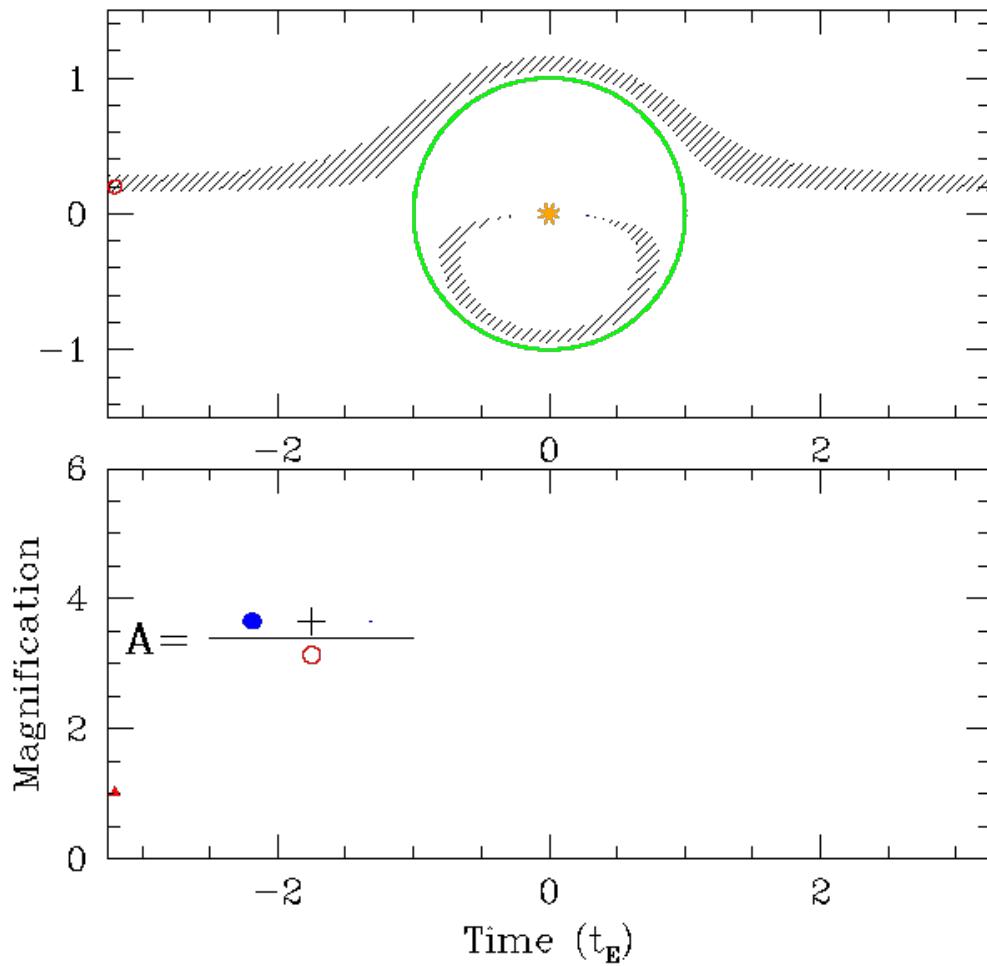


Einstein angle:

$$\theta_E = \sqrt{\frac{4GM_L}{c^2} \left( \frac{1}{D_L} - \frac{1}{D_S} \right)}$$

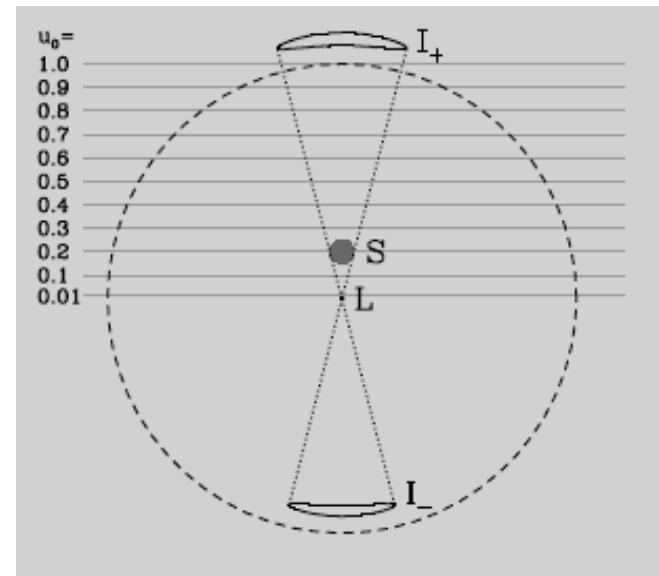


# Microlensing basics



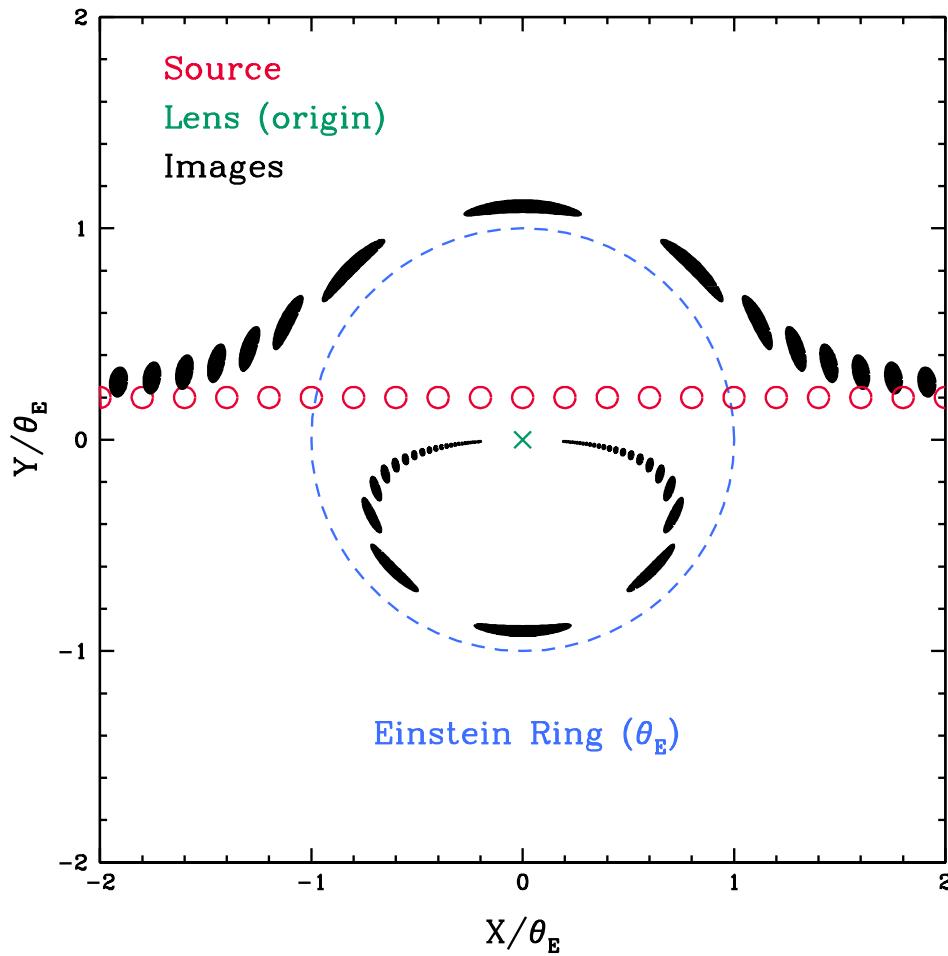
$$A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$$u(t) = \left[ u_0^2 + \left( \frac{t - t_0}{t_E} \right) \right]^{1/2}$$



**S. Gaudi**

# Microlensing basics



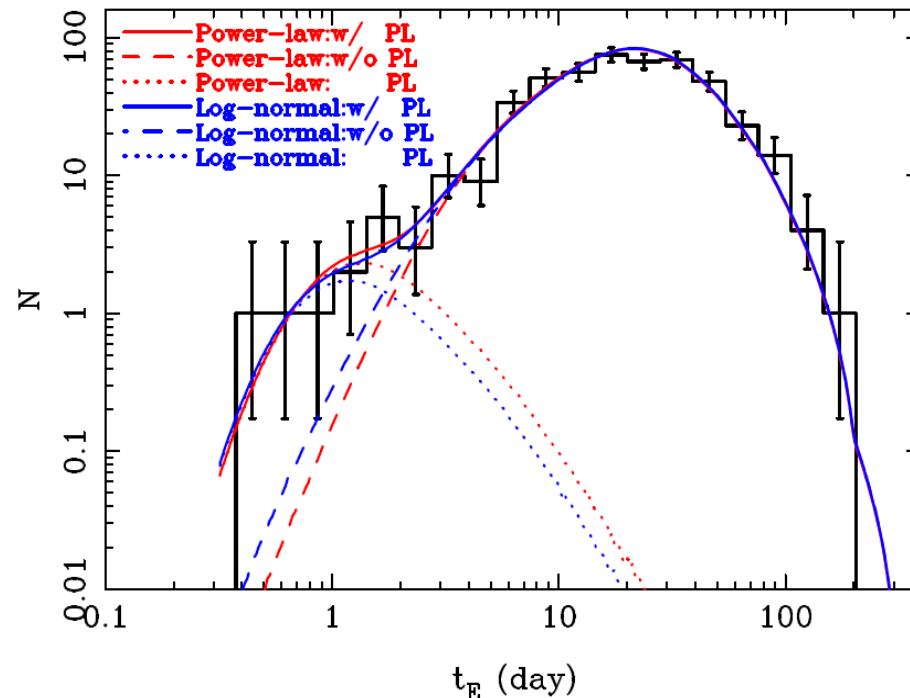
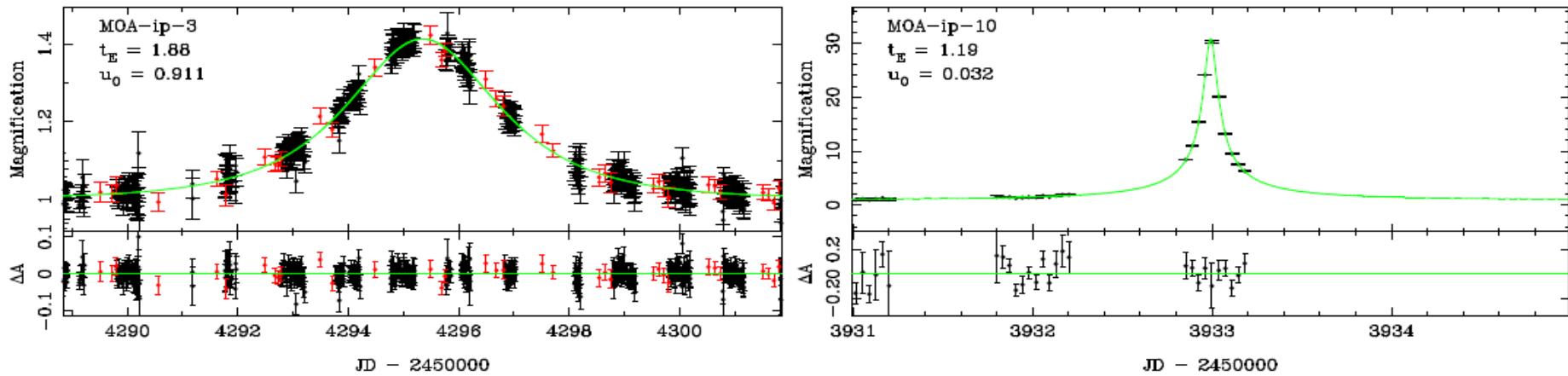
## Event timescale

$$t \downarrow E (M \downarrow L, D \downarrow L, D \downarrow S, \mu \downarrow rel) =$$

$\approx 20$  d for  $0.3 M \downarrow \odot$

$\approx 1$  d for  $M \downarrow J$

# Free floating planets



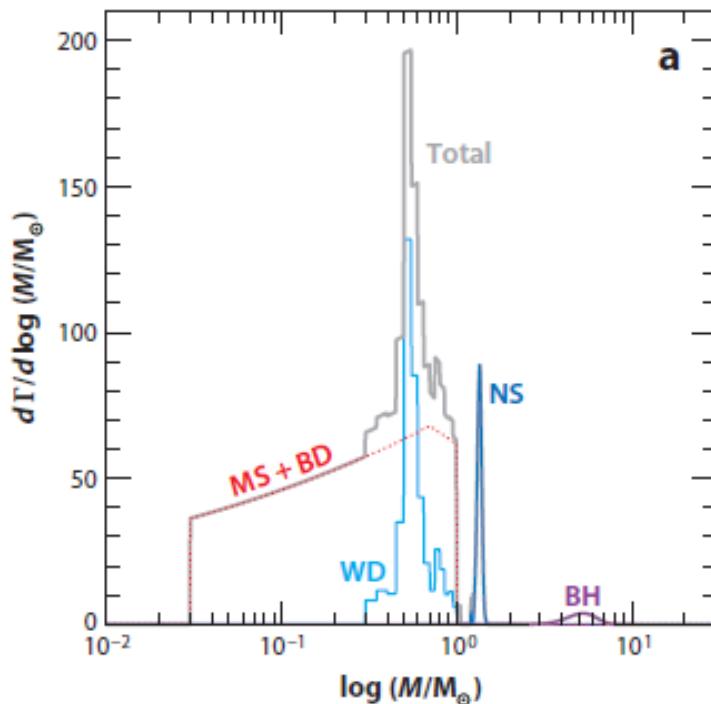
Sumi et al. 2011

# Free floating planets

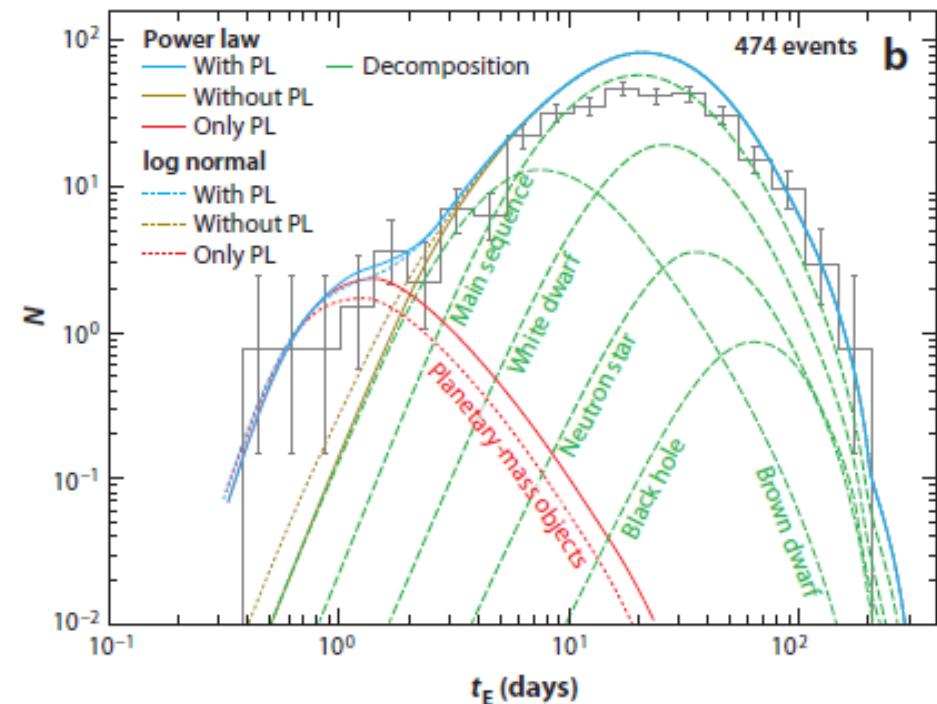
Sumi et al. 2011:

Unbound or distant Jupiters are twice ( $1.8^{+1.7}_{-0.8}$ ) as common as main sequence stars

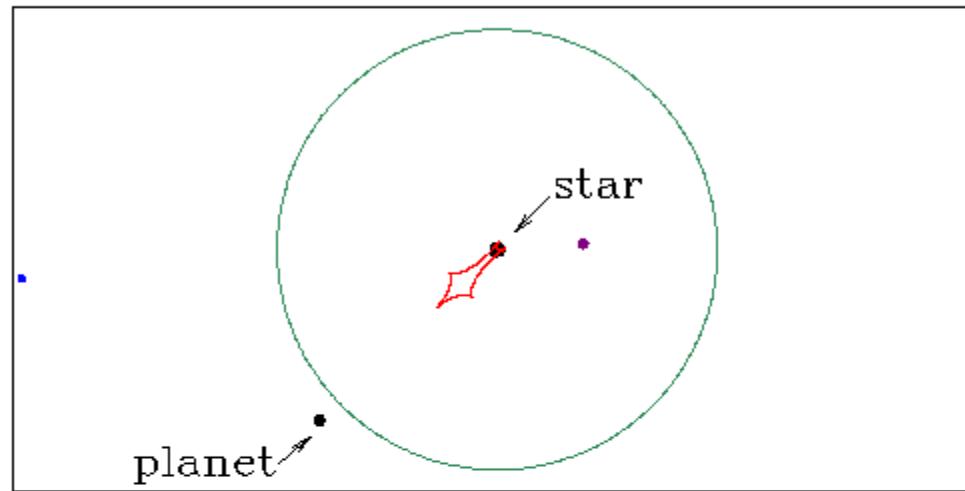
Gould 2000



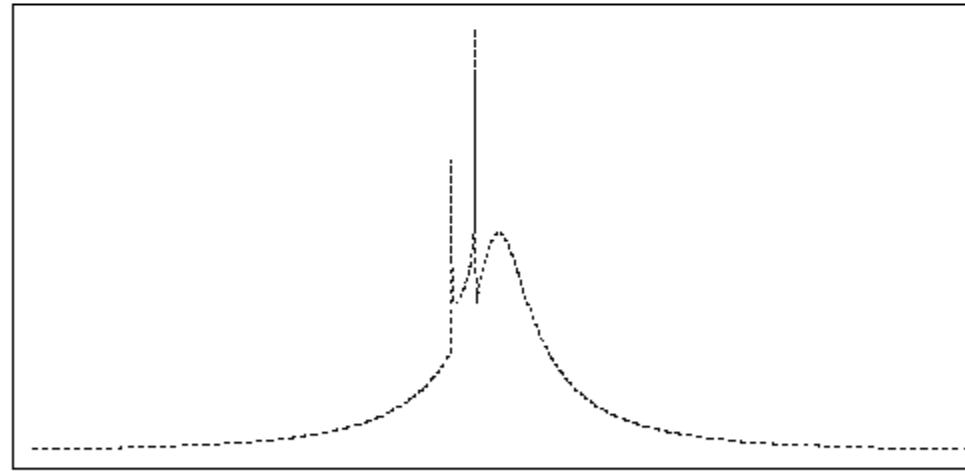
Sumi et al. 2011



# Microlensing basics



Magnification



Time

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# Microlensing basics

## Planet-Star mass ratio

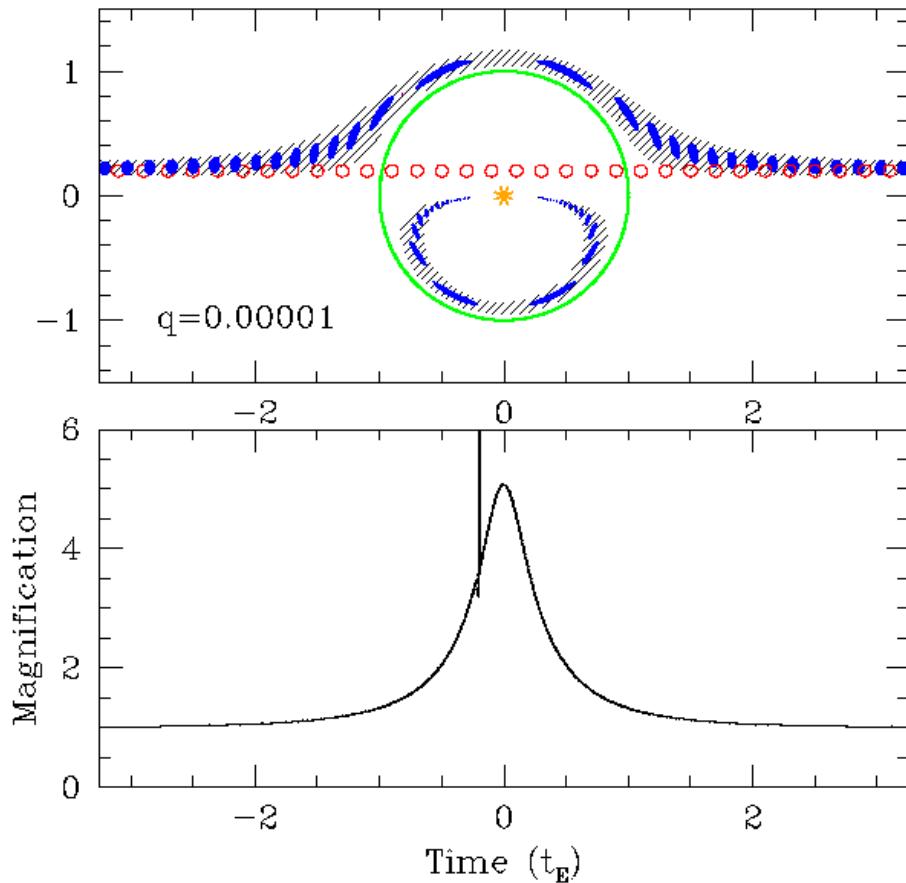
$$q = \frac{M_P}{M_L}$$

## Planet-Star separation

$$s = \frac{a_{\perp}}{r_E}$$

## Event timescale

$$t_E(M_L, D_L, D_S, \mu_{rel}) = \frac{\theta_E}{\mu_{rel}}$$



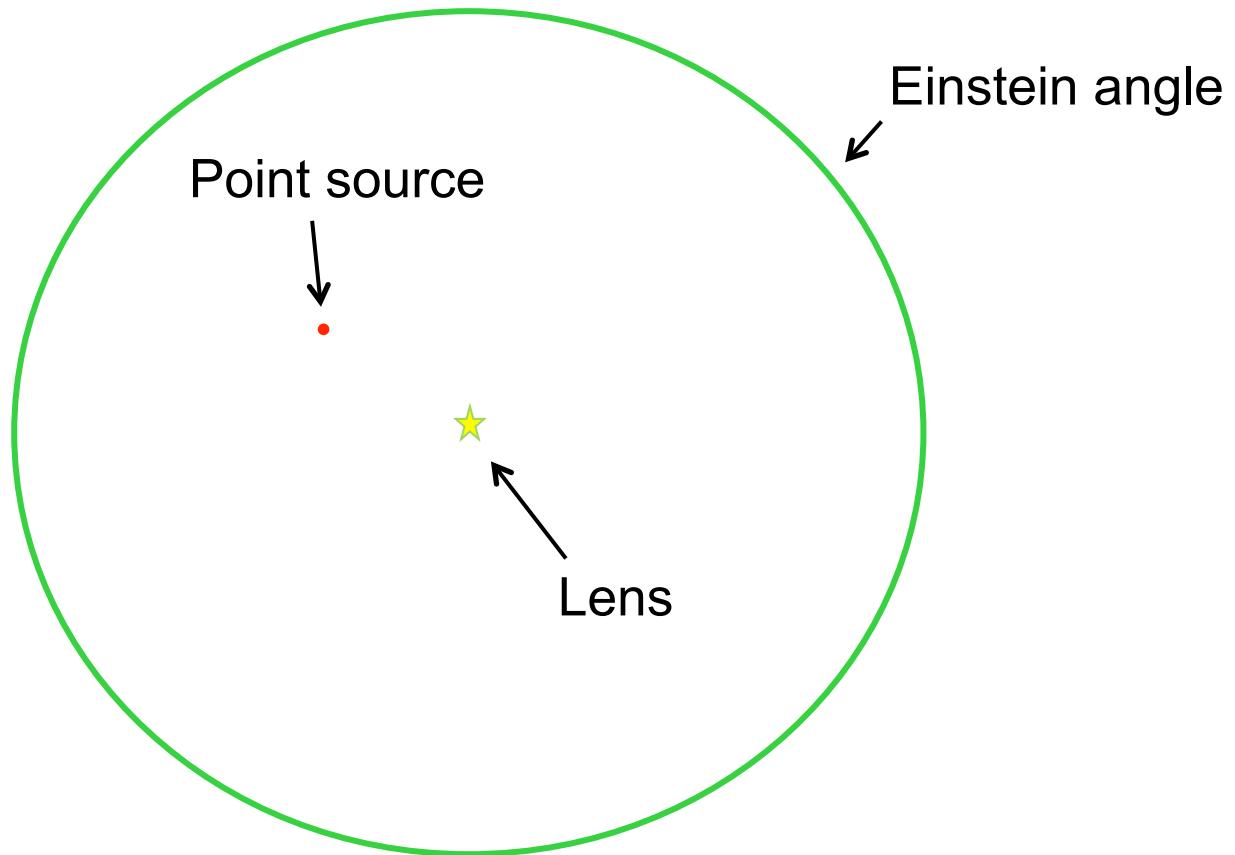
**S. Gaudi**

# From lensing observables to physical parameters

## High order effects:

- Finite source size

$$\rho_* = \frac{\theta_*}{\theta_E}$$

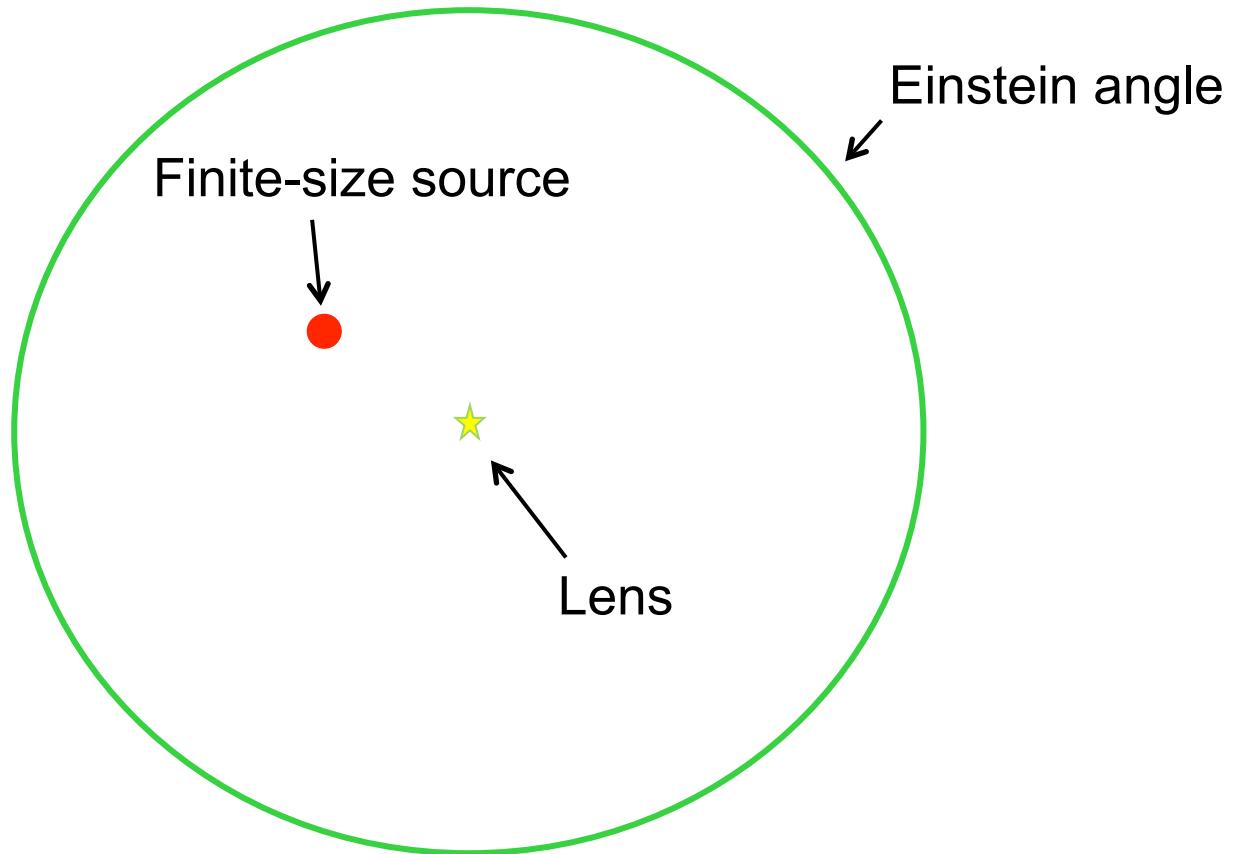


# From lensing observables to physical parameters

## High order effects:

- Finite source size

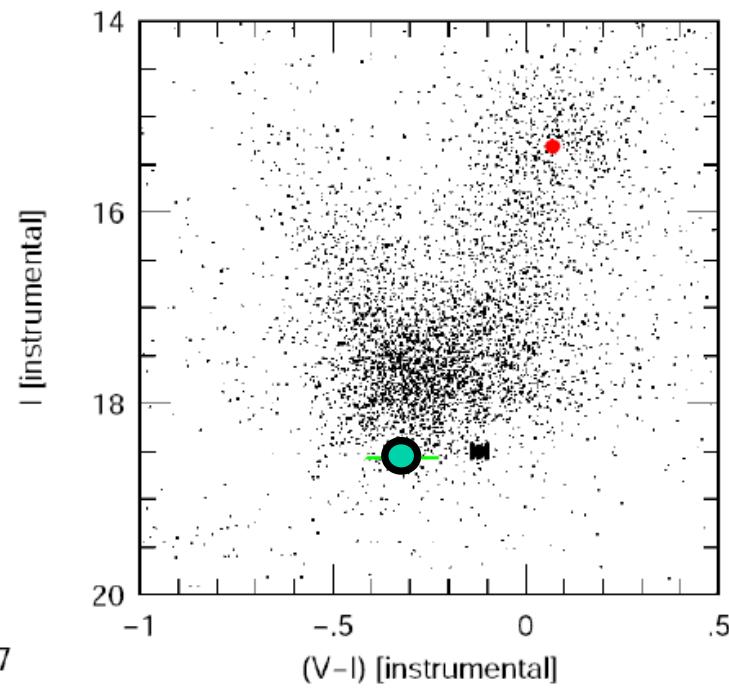
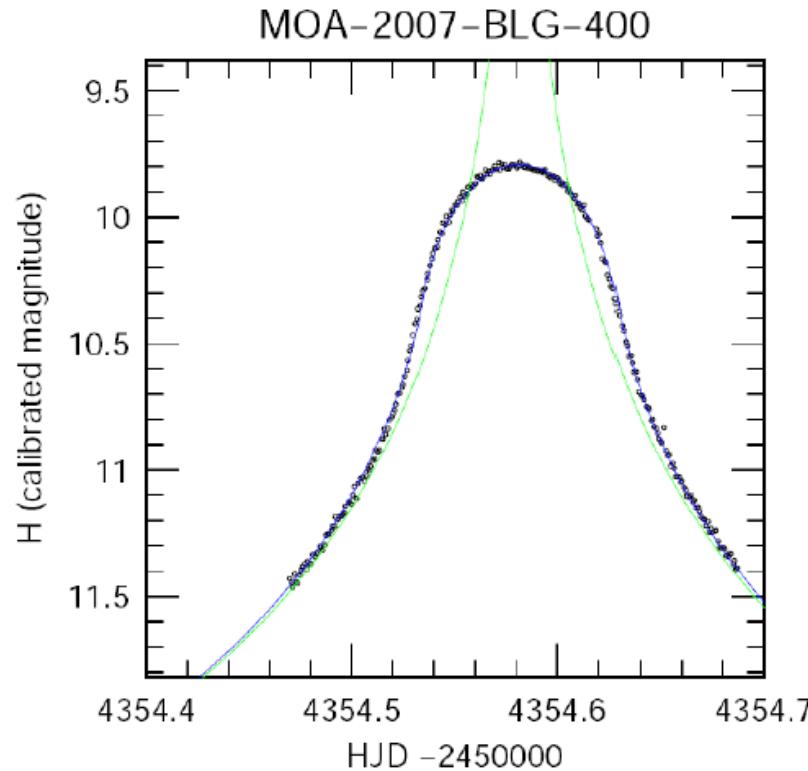
$$\rho_* = \frac{\theta_*}{\theta_E}$$



# From lensing observables to physical parameters

## High order effects:

- Finite source size  $\rho_* = \frac{\theta_*}{\theta_E}$



# From lensing observables to physical parameters

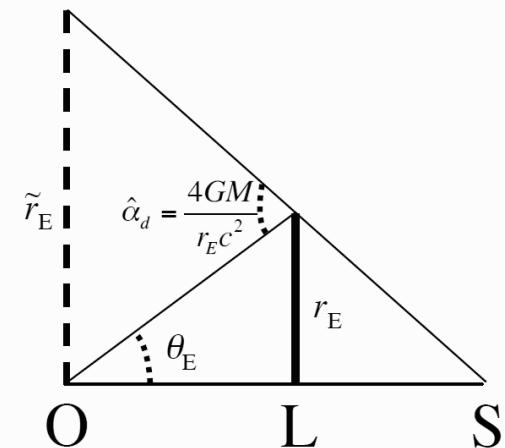
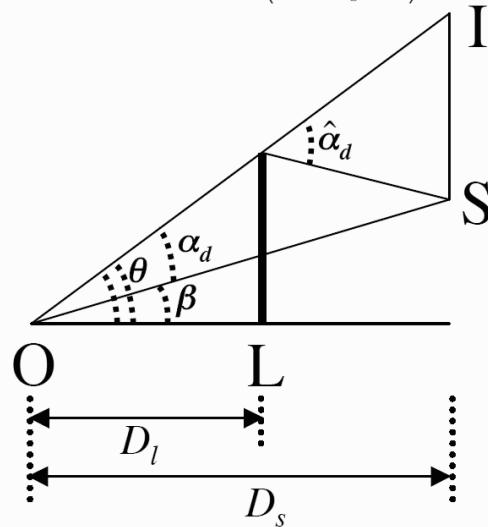
## High order effects:

- Finite source size  $\rho_* = \frac{\theta_*}{\theta_E}$

- Microlens parallax

$$\pi_E = \frac{AU}{\rho_E}$$

$$\beta = \theta - \alpha_d = \theta - \left( \frac{D_s - D_l}{D_s} \right) \hat{\alpha}_d$$



$$\theta_E \tilde{r}_E = \hat{\alpha}_d r_E = \frac{4GM}{c^2}, \quad \frac{\theta_E}{\tilde{r}_E} = D_l^{-1} - D_s^{-1}$$

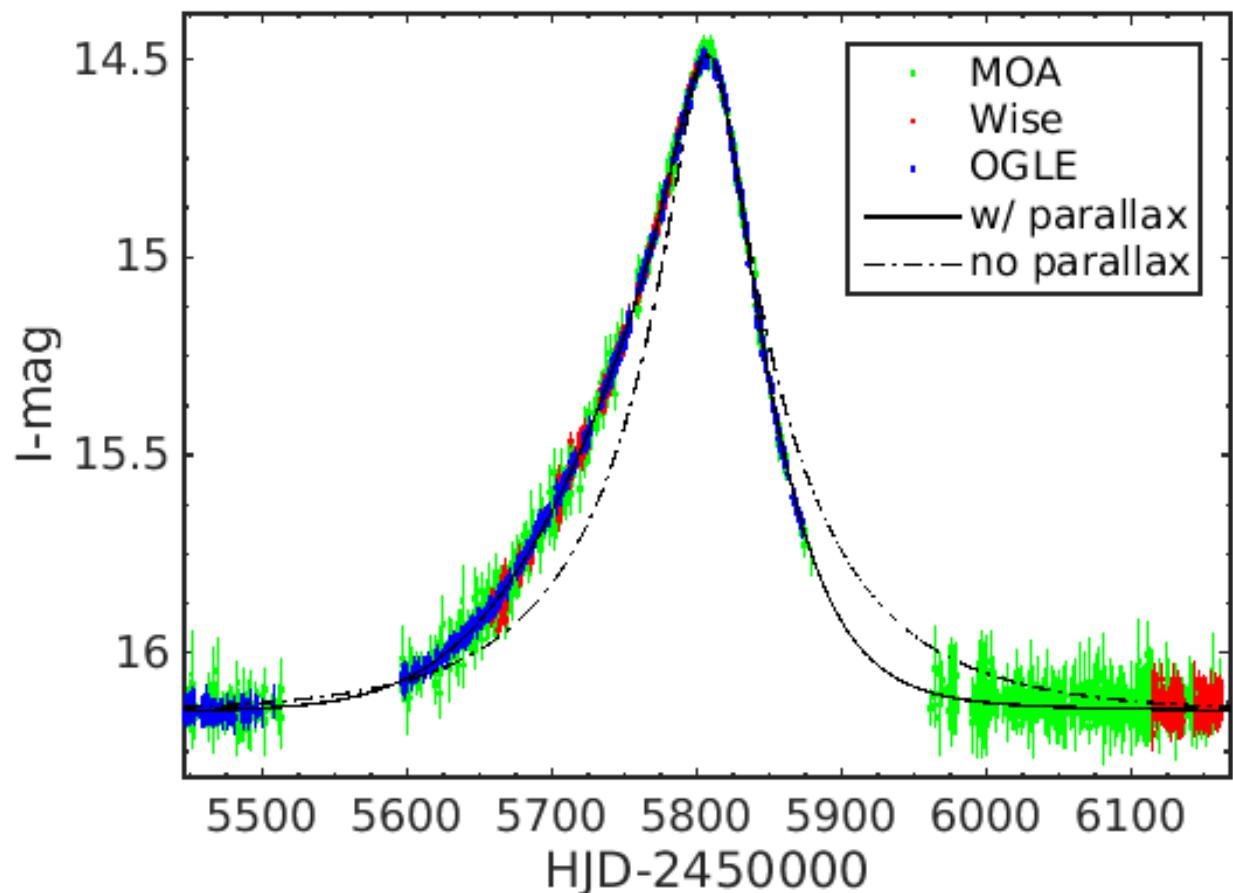
# From lensing observables to physical parameters

## High order effects:

- Finite source size
- Microlens parallax

$$\pi_E = \frac{AU}{\rho_E}$$

## Orbital parallax

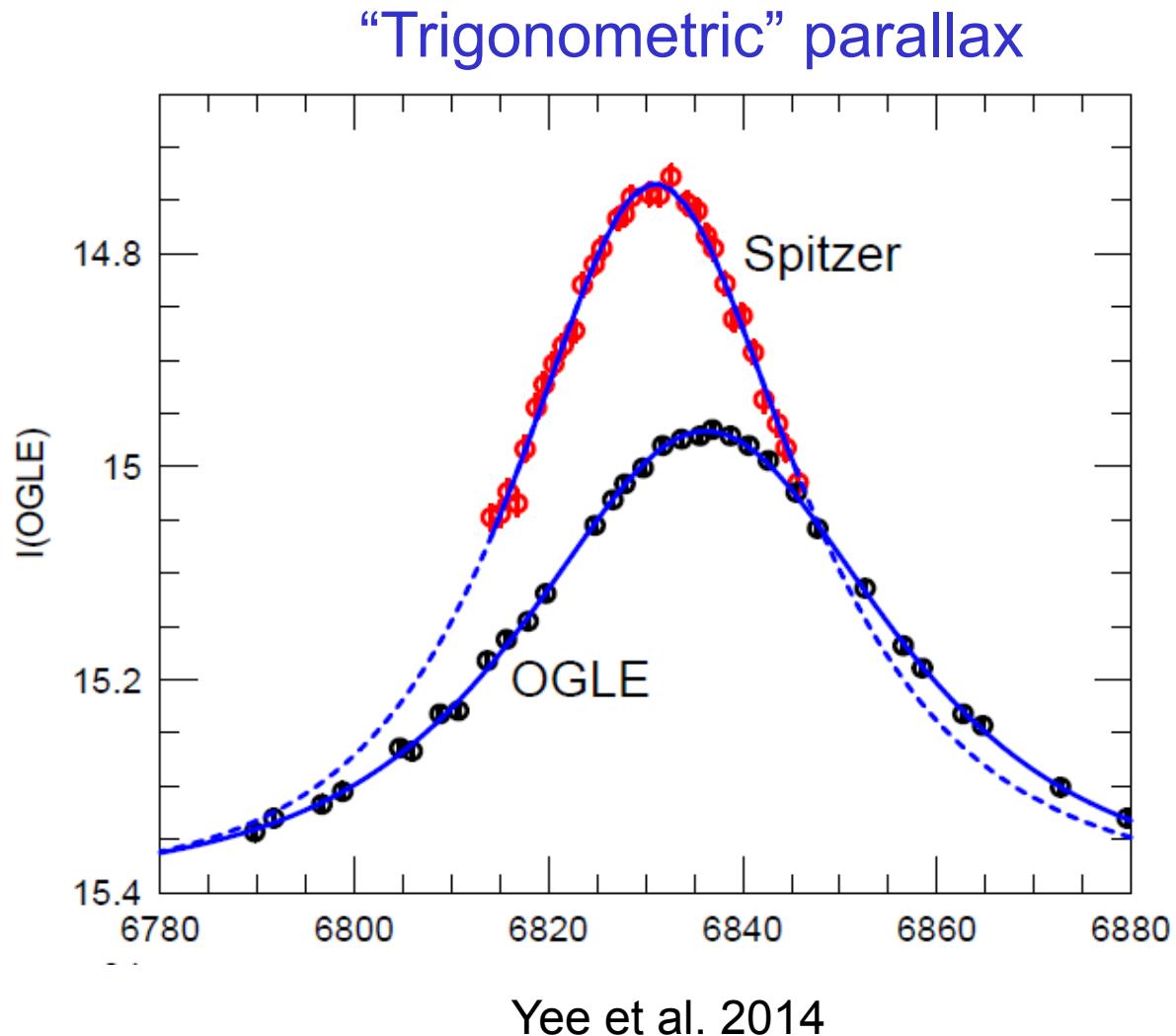


# From lensing observables to physical parameters

## High order effects:

- Finite source size
- Microlens parallax

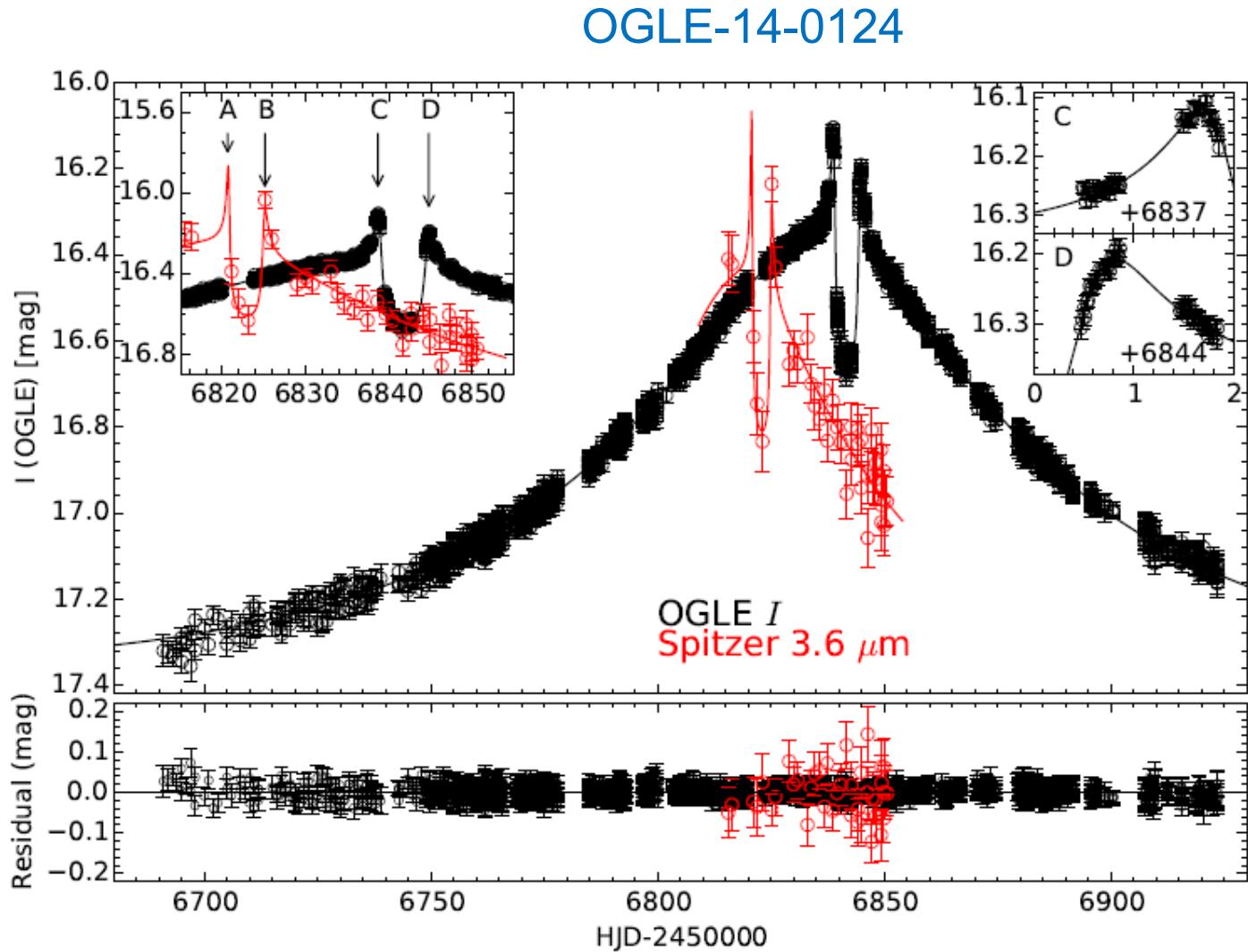
$$\pi_E = \frac{AU}{\rho_E}$$



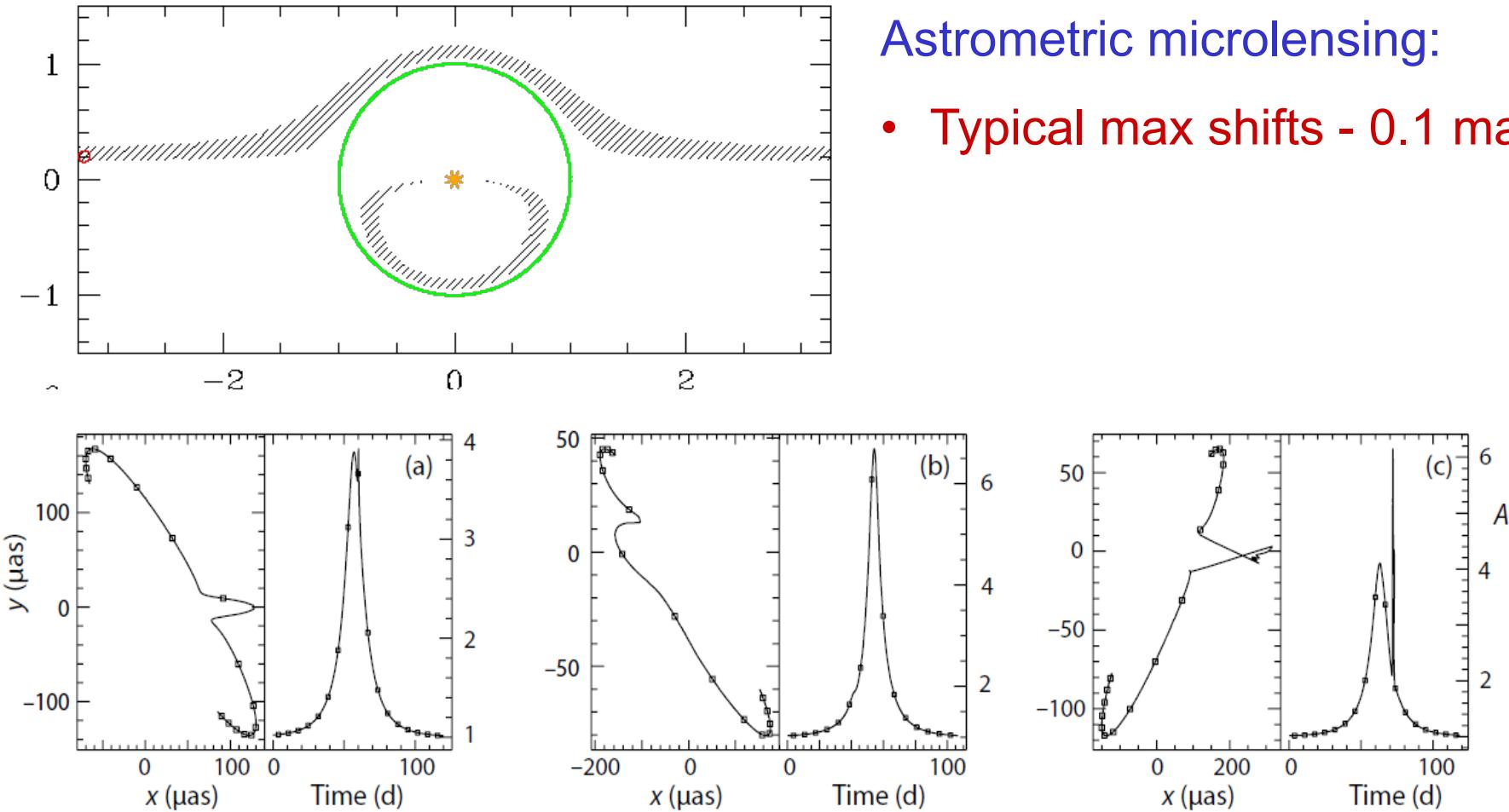
# From lensing observables to physical parameters

$$\begin{aligned}M_P &= 0.51 \pm 0.16 M_J \\a_{\perp} &= 3.11 \pm 0.49 \text{ AU} \\M_L &= 0.71 \pm 0.22 M_e\end{aligned}$$

Udalski et al. 2014



# Astrometric microlensing



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